Ionic Dissociation of Perchloric Acid in Microsolvated Clusters

Kevin H. Weber and Fu-Ming Tao*

Department of Chemistry and Biochemistry, California State University, Fullerton, California 92834 Received: August 11, 2000; In Final Form: November 17, 2000

Ionization or ionic dissociation of perchloric acid in the clusters $HClO_{4-}(H_2O)_n$ (n = 1-3) and $HClO_{4-}NH_{3-}(H_2O)_n$ (n = 0, 1) is investigated by density functional theory and ab initio molecular orbital theory. The equilibrium structures, binding energies, and dipole moments of the clusters are calculated using the hybrid density functional (B3LYP) method with the 6-31+G* and 6-311++G** basis sets and the second-order Møller–Plesset approximation method with the 6-31++G** basis set. Harmonic vibrational frequencies are obtained from the B3LYP/6-311++G** calculations. Perchloric acid is found to require a minimum of three water molecules for ionization to occur and at least one water molecule to protonate ammonia. The corresponding clusters with fewer water molecules are found to be strongly hydrogen-bonded. The acid strength and the related properties of perchloric acid are discussed and compared to those of sulfuric acid in the context of clusters with ammonia and water.

I. Introduction

Acid ionization and acid-base reactions in aqueous solution are probably among the most fundamental processes in chemistry. A common feature in such processes is the transfer of a proton from the acid to the base molecule such as water or ammonia (the proton acceptor). Solvent (water) molecules clearly play a major role in these processes. While experimental insights into the mechanisms of these processes have been limited, quantum mechanical calculations have become a powerful unique tool for investigating such mechanisms in great detail at the molecular level. The mechanisms of ionic dissociation and acid-base reactions have been investigated by computational studies using molecular clusters consisting of the relevant acid, base (proton acceptor), and solvent molecules.¹⁻⁶ The size of the cluster for a given acid or an acid-base pair can be progressively enlarged by adding individual solvent molecules. These studies focus on the specific roles that the individual solvent molecules play and on the minimum number of solvent molecules that are required to cause the ionization of the acid or the transfer of a proton from the acid to the base, a phenomenon that is normally observed or assumed to take place in a liquid solution.

Hydrated clusters involving hydrogen halides (HF and HCl) and H₂S have been shown to require four or more water molecules for ionization to occur.¹ Specifically, hydrogen bromide (HBr) has been shown to have partial ionization with three water molecules and complete ionization with four water molecules.² Ionization of sulfuric acid (H₂SO₄) occurs with as few as three water molecules.^{3,4} Ionization of nitric acid (HNO₃) occurs with five water molecules in the cluster.⁵ In all of these cases one water molecule acts as a proton acceptor while the other water molecules act to stabilize the newly formed ions.

The acid-base neutralization reactions of nitric acid, hydrogen chloride, and sulfuric acid with ammonia in water clusters have also been studied.^{6–8} Although ammonia is regarded as a reasonably strong base, all of the acid-ammonia pairs studied so far show only as hydrogen-bonded complexes in the absence of solvent molecules. Proton transfer occurs for nitric acid– ammonia in a cluster with at least three water molecules,⁶ for hydrogen chloride–ammonia with two water molecules,⁷ and for sulfuric acid–ammonia with only a single water molecule.⁸

All of the clusters mentioned appear to establish the trend that the number of water molecules required for ionization decreases as the acid considered increases in acidity. It is natural then to look at an acid that is considered somewhat stronger than sulfuric acid, the strongest acid previously studied using the approach of clusters. Perchloric acid (HClO₄) is widely considered a stronger acid. In this work, we will examine the clusters of perchloric acid with a varying number of water molecules and the clusters of perchloric acid-ammonia with and without water. The equilibrium geometries, dipole moments, binding energies, and harmonic frequencies for the clusters will be calculated and compared to the corresponding clusters involving sulfuric acid. It would be important for us to analyze any effect of the stronger acid on the properties of the clusters and the number of solvent water molecules required for ionization or proton transfer within a cluster.

Perchloric acid may be important in atmospheric chemistry as well. Svensson et al.⁹ have suggested that perchloric acid may represent an important sink for chlorine between 15 and 20 km above the Earth's surface. Jaegle et al.¹⁰ have also suggested that sulfate aerosol particles may oxidize ClO and form HClO₄, as HCl and HClO₄ have been observed in the reaction of ClO on sulfuric acid.¹¹ Characterization of the molecular properties for the clusters containing HClO₄ may therefore provide valuable insights into the role and significance of the acid in atmospheric chemistry.

II. Theoretical Method

The equilibrium geometries of the molecular clusters considered in this work were optimized by density functional theory (DFT) and ab initio methods. The DFT method used was the popular Becke three-parameter functional^{12–14} with the nonlocal correlation provided by Lee, Yang, and Parr (B3LYP).¹⁵ The ab initio method was frozen-core second-order Møller–Plesset

 $[\]ast$ To whom correspondence should be addressed. E-mail: ftao@fullerton.edu.

perturbation approximation (MP2).^{16,17} Both of the methods are known to be reliable, particularly for calculating closed-shell stable molecules and hydrogen-bonded complexes.^{15,16} All calculations used a reasonably large basis set, 6-311++G(d,p), and were carried out with the Gaussian 98 program package.¹⁸

The molecular clusters $HClO_{4-}(H_2O)_n$ (n = 1-3) and $HClO_{4-}NH_{3-}(H_2O)_n$ (n = 0, 1) were constructed from the three monomers, $HClO_4$, NH_3 , and H_2O . The equilibrium geometries for the monomers and for the clusters were obtained by full optimization using analytic gradients. Our primary focus was on the most stable configuration for each cluster, although other configurations of competing stability were also examined. Generally, the most stable configuration for a cluster contains the strongest possible hydrogen bonding between the monomers. For the larger clusters where the most stable configurations are not obvious, additional calculations were performed on likely candidates to determine the most stable geometry. Our results and discussions, however, are focused on the most stable configurations are mentioned for comparison.

The binding energies of the clusters were also calculated to compare the stability of the clusters with respect to the separate molecules. For a given cluster, the binding energy, $D_{\rm e}$, was determined as a difference between the total energy of the cluster and the sum of the total energies of the isolated monomers (HClO₄, NH₃, and *n*-H₂O) contained in the cluster. Harmonic vibrational frequencies and IR intensities for all clusters were obtained from B3LYP calculations. Zero-point energy-corrected binding energies, D_0 , were obtained using the calculated harmonic frequencies. No corrections were made to $D_{\rm e}$ for the basis set superposition error (BSSE). The effect of BSSE is expected to be relatively small as compared to the binding energy for a strongly hydrogen-bonded system such as HClO₄–NH₃–(H₂O)_n. A previous study⁵ on a similar system, NH₃₋HNO₃, using the same method showed that the BSSE contribution was less than 0.4 kcal/mol, compared to a value of 14 kcal/mol for the binding energy $D_{\rm e}$.

III. Results and Discussion

Figures 1 and 2 show side views of the equilibrium structures for the clusters $HClO_{4-}(H_2O)_n$ (n = 1-3) and $\text{HClO}_{4-}\text{NH}_{3-}(\text{H}_{2}\text{O})_{n}$ (n = 0, 1), respectively. Table 1 gives the bond distances, bond angles, dipole moments, and total energies of the relevant monomers (NH₃, NH₄⁺, HClO₄, ClO₄⁻, H₂O, and H₃O⁺), compared with available experimental data.^{19,20} Tables 2 and 3 present selected bond lengths and molecular properties of the two cluster series, $HClO_{4-}(H_2O)_n$ (n = 1-3) and $HClO_4-NH_3-(H_2O)_n$ (n = 0, 1), respectively. It is clear from the tables that the B3LYP and MP2 calculations are consistent with each other. Nevertheless, the following discussions of these results are primarily based on the MP2 values. Table 4 presents the harmonic vibrational frequencies and infrared intensities for the intramolecular modes of the clusters from B3LYP calculations, compared to and correlated with those of HClO₄, ClO₄⁻, H₃O⁺, and NH₄⁺, along with available experimental values.²⁰ Note that the frequencies for the monomers H₂O and NH₃ are reported elsewhere^{4,8} and the corresponding intramolecular frequencies are not significantly different from these monomer frequencies.

Monomers. As shown in Tables 1 and 4, the equilibrium geometry and molecular properties calculated for perchloric acid are in reasonable agreement with experiment values.²¹ The hydrogen atom of HClO₄ is staggered from the rest of the molecule, and the base of the molecule (ClO₃) is close to $C_{3\nu}$



Figure 1. Equilibrium geometries for the clusters $HClO_{4-}(H_2O)_n$ (n = 1-3) from B3LYP calculations.



Figure 2. Equilibrium geometries for the clusters $HClO_4-NH_3-(H_2O)_n$ (*n* = 0, 1) from B3LYP calculations.

HClO₄-NH₃-H₂O

HClO₄-NH₃

symmetry. The equilibrium geometry is also in agreement with previous calculations.^{22,23} The equilibrium geometries for water and ammonia are also in good agreement with experiment.⁸ The calculated dipole moments are overestimated, but are consistent with the level of theory and basis sets used in this study.⁶

The calculated harmonic frequencies of perchloric acid agree reasonably with available experimental values and with the MP2

TABLE 1: Equilibrium Bond Distances (Å), Bond Angles (deg), Dipole Moments (D), and Total Energies (hartrees) Calculated for Monomeric HClO₄, ClO₄⁻, H₂O, H₃O⁺, NH₃, and NH₄⁺ from Different Calculations and Experiment

molecule ^a	param	B3LYP	MP2	$exptl^b$
$HClO_4(C_s)$	<i>r</i> (O1H)	0.974	0.973	0.98^{c}
	r(ClO1)	1.726	1.704	1.641
	r(ClO2)	1.460	1.439	1.414
	r(ClO3)	1.460	1.439	1.414
	<i>r</i> (ClO4)	1.449	1.429	1.404
	∠(ClO1H)	105.5	105.4	105.0
	μ	2.28	2.08	
	Ε	-761.41835	-759.15290	
$\text{ClO}_4^-(T_d)$	r(ClO)	1.501	1.476	
	∠(OClO)	109.500	109.5	
	μ	0.00	0.00	
	E	-760.93252	-758.68037	
$H_2O(C_{2v})$	r(OH)	0.980	0.978	0.957
	∠(HOH)	113.5	112.1	104.5
	μ	2.16	2.26	1.94
	E	-76.45853	-76.05260	
$H_3O^+(C_{3v})$	r(OH)	0.980	0.978	
	∠(HOH)	113.5	112.1	
	μ	1.44	1.57	
$NH_3(C_{3v})$	$r(\rm NH)$	1.015	1.013	1.012
	∠(HNH)	107.8	107.4	106.7
	μ	1.69	1.73	1.51
	Ε	-56.58272	-56.21435	
$\rm NH_{4}^{+}$ ($T_{\rm d}$)	$r(\rm NH)$	1.026	1.024	
	∠(HNH)	109.5	109.5	
	μ	0.00	0.00	
	Ε	-56.92036	-56.75569	

^{*a*} Some of the atomic labels have been omitted due to uniqueness or symmetry. ^{*b*} Experimental values for NH₃ and H₂O are from ref 19, and those for HClO₄ are from ref 22. ^{*c*} Not refined.

TABLE 2: Equilibrium Bond Lengths (Å), Rotational Constants *A*, *B*, and *C* (GHz), Binding Energies D_e (kcal/mol), and Dipole Moments μ (D) of the HClO₄-(H₂O)_n (n = 1-3) System from B3LYP and MP2 Calculations

	HClO ₄₋ H ₂ O		HClO ₄₋	(H ₂ O) ₂	$HClO_{4-}(H_2O)_3$		
param	B3LYP	MP2	B3LYP	MP2	B3LYP	MP2	
<i>r</i> (O1H1)	1.002	0.995	1.031	1.019	1.549	1.497	
r(H1O5)	1.679	1.696	1.536	1.551	1.026	1.030	
<i>r</i> (ClO1)	1.684	1.655	1.637	1.631	1.536	1.514	
r(ClO2)	1.466	1.444	1.478	1.455	1.502	1.477	
r(ClO3)	1.466	1.445	1.464	1.443	1.502	1.477	
<i>r</i> (ClO4)	1.451	1.430	1.450	1.430	1.458	1.437	
r(H2O5)	0.964	0.962	0.963	0.961	1.023	1.012	
r(H3O5)	0.964	0.962	0.985	0.978	1.023	1.012	
<i>r</i> (O7H3)			1.746	1.765	1.550	1.560	
r(O7H4)			0.970	0.966	0.980	0.976	
r(O7H5)			0.962	0.960	0.963	0.961	
<i>r</i> (O2H4)			2.018	2.014	1.832	1.832	
r(O6H2)					1.550	0.960	
r(O6H6)					0.980	0.976	
r(O6H7)					0.963	0.961	
r(O3H6)					1.832	1.832	
Α	4.954	5.099	3.027	3.093	1.813	1.845	
В	1.843	1.964	1.259	1.290	1.085	1.103	
С	1.816	1.934	1.082	1.107	0.861	0.878	
μ	4.66	4.10	4.08	3.76	5.79	5.6	
$D_{\rm e}$	12.0	13.9	24.5	24.0	37.7	34.3	

values by Francisco et al.²³ The experimental frequencies that were compared in the early theoretical study²³ were inaccurate due to Cl₂O₇ impurities.²⁴ A procedure was developed to remove the Cl₂O₇ impurities and resulted in more reliable experimental frequencies for the v_2 , v_3 , v_9 , and v_{11} modes shown in Table 4.²⁵ This indicates the degree of uncertainty and challenge in determining the spectral data for perchloric acid as the acid is highly reactive and unstable.

TABLE 3: Equilibrium Bond Lengths (Å), Rotational Constants *A*, *B*, and *C* (GHz), Binding Energies D_e (kcal/mol), and Dipole Moments μ (D) of the HClO₄–NH₃–(H₂O)_n (n = 0, 1) from B3LYP and MP2 Calculations

	HClO4	-NH ₃	HClO ₄₋ N	HClO ₄ -NH ₃ -H ₂ O		
param	B3LYP	MP2	B3LYP	MP2		
<i>r</i> (NH1)	1.582	1.582	1.061	1.061		
r(NH2)	1.016	1.016	1.052	1.047		
r(NH3)	1.017	1.017	1.017	1.016		
r(NH4)	1.017	1.017	1.022	1.019		
r(ClO1)	1.657	1.632	1.532	1.507		
r(ClO2)	1.454	1.432	1.462	1.441		
r(ClO3)	1.469	1.447	1.501	1.477		
r(ClO4)	1.470	1.445	1.505	1.480		
r(O1H1)	1.049	1.033	1.676	1.629		
r(O3H4)	3.456	3.102	2.406	2.478		
r(O5H5)			0.983	0.978		
r(O5H6)			0.962	0.960		
r(O5H2)			1.711	1.698		
r(O2H5)			1.820	1.816		
Α	4.977	5.126	3.037	3.105		
В	1.845	1.956	1.428	1.463		
С	1.822	1.930	1.197	1.223		
μ	6.40	5.81	9.23	9.21		
$D_{\rm e}$	17.0	17.8	32.6	35.5		

 $HClO_{4-}(H_2O)_n$ Structures. A strong hydrogen bond forms in HClO₄-H₂O as the first water is introduced to perchloric acid. The acid acts as a hydrogen bond donor while the water acts as an acceptor in this monohydrated cluster. The interaction between perchloric acid and water is highly strong and rigid, with a short and nearly linear O-H-O hydrogen bond. The strong hydrogen bonding of perchloric acid to water is also evidenced by the increase of the acidic OH bond distance, r(O1H1), from 0.973 to 0.995 Å, accompanied by a red shift in the OH stretching frequency and a sharp increase in IR intensity (to be discussed in detail later). The binding energy between the acid and the water in HClO₄-H₂O is 13.9 kcal/mol at the MP2 level (12.0 kcal/mol at B3LYP). It should be noted that two possible equilibrium structures are observed for this cluster that are very similar in energy. The structural difference arises from the orientation of the water molecule, having one pointing away from the O atoms of perchloric acid and the other pointing toward the O atoms. The slightly more stable structure, as reported, can lead to the ionic dissociation of the acid by adding two more water molecules while the other structure cannot lead to the dissociation.

In the dihydrated cluster, $HClO_{4-}(H_2O)_2$, the second water molecule is oriented in such a way that it accepts a hydrogen bond from the first water while donating a hydrogen bond to an oxygen atom of perchloric acid. As a result, a cyclic hydrogen bond ring structure is established. The bond distance between the H atom of $HClO_4$ and the O atom of the first water, r(H1O5), decreases to 1.551 Å from 1.696 Å for $HClO_4-H_2O$, while the O-H covalent bond distance of HClO₄, r(O1H1), increases further to 1.019 Å from 0.995 Å for HClO₄–H₂O. This indicates that the hydrogen bond of the $HClO_4-H_2O$ unit in $HClO_4-(H_2O)_2$ is further strengthened while the O-H covalent bond of HClO₄ is weakened. There are two additional hydrogen bonds in $HClO_{4-}(H_2O)_2$. One is between the first and second water molecules. The bond distance r(O7H3) = 1.77 Å indicates that it is nearly as strong as the hydrogen bond for HClO₄-H₂O. The other hydrogen bond is between the second water and the oxygen of perchloric acid. The bond distance r(O2H4) = 2.01Å indicates it is a weaker and more typical hydrogen bond. The binding energy for HClO₄₋(H₂O)₂ is over 10 kcal/mol larger than that for HClO₄-H₂O, consistent with the existence of two

TABLE 4: Harmonic Frequencies (cm⁻¹) and Infrared Intensities (km/mol, in Parentheses) of $HClO_{4-}(H_2O)_n$ (n = 0-3) and $HClO_{4-}NH_{3-}(H_2O)_n$ (n = 0, 1) from B3LYP Calculations, Correlated by Monomer Vibrational Modes

monomer		freq for monomer		free	q for HClO ₄₋ (H ₂	$O)_n$	freq for HClO ₄ –NH ₃ –(H ₂ O	
mode	approx descriptn	calcd	exptl	n = 1	n = 2	n = 3	n = 0	n = 1
$v_1(a)$	OH str ClO asym str	3707 (133)	3553	HClO ₄ 3181 (1339) 1101 (308)	a 2548 (2189) 1107 (208)		2349 (3004)	
$v_2(a) = v_3(a)$	HOCl bend	1122 (209) 1118 (146)	1201	1376 (91)	1474 (90)		1538 (70)	
v_4 (a) v_5 (a)	ClO sym str Cl-OH str	936 (93) 644 (169)	726	928 (121) 671 (158)	694 (130)		692 (5)	
$ \nu_{6}(a) \nu_{7}(a) $	OClO asym def OClO sym def	518 (27) 478 (1)	582 555	523 (10) 498 (8)	532 (17) 512 (34)		535 (4) 518 (22)	
$ \nu_8 (a) \nu_9 (b) $	ClO3 rock ClO asym str	357 (4) 1232 (156)	421 1265	366 (0) 1134 (220)	363 (1) 1041 (205)		391 (3) 1128 (278)	
ν_{10} (b) ν_{11} (b) ν_{12} (b)	OClO asym def ClO3 rock OH torsion	514 (25) 363 (20) 179 (86)	582 421	524 (21) 386 (3) 895 (75)	576 (84) 397 (43) 943 (239)		528 (23) 372 (45) 1131 (262)	
ClO_4^- $v_1(e)$	<i>d</i> -str	397 (16)				413 (18)		387 (11)
$v_2(t)$	<i>d</i> -def	555 (21)				418 (10) 551 (20) 562 (10) 571 (685)		434 (13) 549 (22) 551 (19) 568 (32)
$ \begin{array}{l} \nu_{3}\left(a_{1} ight) \\ \nu_{4}\left(t ight) \end{array} $	sym str d-def	806 (6) 971 (359)				791 (170) 959 (368) 937 (78) 850 (239)		794 (76) 1084 (346) 957 (300) 900 (299)
				H_3O^+				
$\nu_1 \\ \nu_2 \\ \nu_3 \\ \nu_4$	sym def <i>d</i> -def sym str <i>d</i> -str	765 (518) 1673 (121) 1673 (121) 3584 (40) 3680 (498) 2690 (498)				764 (5) 1789 (87) 1734 (47) 2947 (881) 2658 (1406) 2727 (2045)		
		3080 (498)		NILL +/	,	2727 (2045)		
$ \nu_1 (a_1) \\ \nu_2 (e) $	sym str <i>d</i> -def	3371 (7) 1728 (2)	3115 1638	INH4''				3478 (116) 1738 (44) 1730 (36)
$\nu_{3}(t)$	<i>d</i> -str	3475 (183)	3250					3572 (85) 2975 (805) 2827 (968)
$\nu_{4}\left(t ight)$	<i>d</i> -def	1490 (163)	1398					1412 (61) 1484 (100) 1591 (283)

^a Experimental frequencies from refs 21, 24, and 25. ^b Experimental frequencies in solid NH₄VO₃ from ref 26.

additional hydrogen bonds in $HClO_4-(H_2O)_2$. Note that the second water removes the C_s symmetry in the $HClO_4-H_2O$ unit.

The equilibrium structure for the trihydrated cluster, $HClO_{4-}(H_2O)_3$, is drastically different from that for the smaller clusters discussed above. The perchloric acid in HClO₄₋(H₂O)₃ is spontaneously dissociated into hydrated ions. The third water takes a position at the opposite side of the HClO₄₋H₂O unit from the second water, donating a hydrogen bond to the O3 atom of $HClO_4$ and restoring the C_s symmetry to the system. The O1H1 bond distance increases from 1.02 to 1.50 Å while the H1O5 bond distance decreases from 1.55 to 1.03 Å as a result of the addition of the third water. It is clear that the O1H1 covalent bond no longer exists and a new O5H1 covalent bond is formed. The ion pairs ClO_4^- and H_3O^+ form as a proton is transferred from HClO₄ to H₂O. The formation of the ion pair is also indicated by an increase in the dipole moment, from 4.10 to 5.63 D, as well as the significant departure of the O1-H1-O5 unit from linearity expected for a typical hydrogen bond. A large binding energy is calculated for HClO₄₋(H₂O)₃, about 10 kcal/mol larger than that for $HClO_{4-}(H_2O)_2$. This is consistent with the stable structure of $HClO_{4-}(H_2O)_3$ that displays favorable interactions of ion pair and polar water molecules.

HClO₄–NH₃–(H₂O)_{*n*} **Structures.** Perchloric acid is a very strong acid, and ammonia is a reasonably strong base. Surprisingly, the union of the two, HClO₄–NH₃, exists only as a strongly hydrogen-bonded complex, with HClO₄ acting as the hydrogen bond donor and NH₃ as the acceptor. The hydrogen bond distance, r(NH1) = 1.582 Å, is shorter than r(H1O5) = 1.696 Å for HClO₄–H₂O and is comparable to that of the sulfuric acid–ammonia cluster (1.579 Å).¹⁰ The O–H covalent bond distance, r(O1H1) = 1.033 Å, is about 0.06 Å longer than the O–H bond distance of HClO₄.

In the monohydrated cluster, $HClO_4-NH_3-H_2O$, a drastic change in geometry takes place at the $HClO_4-NH_3$ unit. The introduction of one water molecule to $HClO_4-NH_3$ facilitates the proton transfer from $HClO_4$ to NH_3 , forming the ion pair $NH_4^{+}-ClO_4^{-}$. The water molecule is so orientated that a H atom connects to an oxygen atom (O4) of ClO_4^{-} while the O atom of H_2O connects to a H atom of NH_3 . The *r*(O1H1) distance increases from 1.033 to 1.629 Å and the distance *r*(NH1) decreases from 1.582 to 1.061 Å as a result of the addition of the H_2O molecule. Clearly, the O–H covalent bond of $HClO_4$ no longer exists, and a new NH1 covalent bond is formed. The NH₃ unit rotates noticeably as it converts to the NH_4^+ cation, and multiple hydrogen bonds form in the $HClO_4-NH_3-H_2O$

TABLE 5: Comparison of Selected Bond Lengths (Å), Binding Energies (kcal/mol), Harmonic Frequencies (cm⁻¹) and Infrared Intensity (km/mol, in Parentheses) for the Clusters $HClO_4$ -H₂O, H₂SO₄-H₂O,^{*a*} $HClO_4$ -NH₃-(H₂O)_{*n*} (*n* = 0, 1) and H₂SO₄-NH₃-(H₂O)_{*n*} (*n* = 0, 1)^{*b*}

param	theory	HClO ₄	H_2SO_4	HClO ₄₋ H ₂ O	$\begin{array}{c} H_2SO_{4-} \\ H_2O \end{array}$	HClO ₄₋ NH ₃	H ₂ SO ₄₋ NH ₃	HClO ₄₋ NH ₃₋ H ₂ O	$\begin{array}{c} H_2SO_{4-} \\ NH_{3-}H_2O \end{array}$
r(O1H1)	B3LYP	0.974	0.970	1.002	0.999	1.049	1.043	1.676	1.464
	MP2	0.973	0.968	0.995	0.992	1.033	1.035	1.629	1.444
r(H1O5)	B3LYP			1.679	1.692				
	MP2			1.696	1.701				
<i>r</i> (H1N)	B3LYP					1.582	1.586	1.061	1.106
	MP2					1.582	1.579	1.061	1.105
∠(O−H•••O(N))	B3LYP			175	163	179	173	158	177
$D_{\rm e}$	B3LYP			12.0	12.4	17.0	16.5	32.6	30.3
	MP2			13.9	13.3	17.8	16.4	35.5	35.5
D_0	B3LYP			9.98	10.2	15.1	14.7	26.7	25.37
ν_1 OH stretch	B3LYP	3707 (133)	3757 (198)	3181 (1339)	3199 (1214)	2349 (3004)	2538 (2863)		
ν_1 red shift	B3LYP			526	502	1358	1256		
ν_1 IR ratio	B3LYP			10	6	23	14		
ν_{12} OH torsion	B3LYP	179 (86)	260 (78)	895 (75)	827 (75)	1131 (262)	1137 (140)		
v_{12} blue shift	B3LYP			716	567	952	877		
ν_3 HO···Cl(S) bend	B3LYP	1118 (146)	1128 (96)	1376 (91)	1310 (102)	1538 (70)	1491 (114)		
v_3 blue shift	B3LYP			258	182	420	363		

^a Reference 4. ^b Reference 8.

cluster. The ClO₄⁻ unit also rotates to maximize the electrostatic interaction with NH₄⁺. The rotations of NH₄⁺ and ClO₄⁻ are shown by the change in the distance between the O4 and H4 atoms. This distance decreases from 3.456 Å in HClO₄–NH₃ to 2.406 Å in HClO₄–NH₃–H₂O. The rotations would not be possible if the structure of the cluster were dominated by hydrogen bonding. The formation of the ion pair NH₄⁺••ClO₄⁻ in HClO₄–NH₃–H₂O is evidenced by a sharp increase in dipole moment, from 5.81 D for HClO₄–NH₃ to 9.21 D HClO₄–NH₃–H₂O. The binding energy is $D_e = 17.8$ kcal/mol for HClO₄–NH₃ and $D_e = 35.5$ kcal/mol for HClO₄–NH₃–H₂O. The addition of the water molecule results in an increase of 17.7 kcal/mol in D_e .

 $HClO_{4-}(H_2O)_n$ and $HClO_{4-}NH_{3-}(H_2O)_n$ Frequencies. With some exceptions, there are no significant changes in the intramolecular vibrational frequencies for the clusters HClO₄-H₂O, $HClO_4-(H_2O)_2$, and $HClO_4-NH_3$ from those for the isolated monomers. This supports the equilibrium structures and the fact that no significant changes in bonding take place in the clusters from the monomers. The exceptions are all related to the vibrational modes involving the H atom of HClO₄. Three specific modes are involved: the OH stretching (v_1) , the HOCl bending (v_3) , and the O-H torsion (v_{12}) , all of which result in significant changes in frequency from the monomer to the clusters. In the cluster HClO₄₋H₂O, the OH stretching mode shifts from 3707 to 3181 cm⁻¹ while IR intensity increases by an order of magnitude. For HClO₄₋(H₂O)₂, the OH stretching mode further shifts to 2548 cm⁻¹, with a 2-fold enhancement in IR intensity. Similarly, the OH stretching mode for HClO₄-NH₃ shifts to 2349 cm⁻¹ with a 23-fold enhancement in IR intensity. This is consistent with the weakening of the OH bond in these clusters as a result of strong hydrogen bonding. On the other hand, the bending and torsional modes for perchloric acid undergo significant blue shifts in these clusters. More specifically, the HOCl bending frequency (v_3) increases from 1118 cm^{-1} for the HClO₄ monomer to 1376, 1474, and 1538 cm^{-1} for HClO₄–H₂O, HClO₄–(H₂O)₂, and HClO₄–NH₃, respectively. Similarly, the OH torsional frequency (v_{12}) increases from 179 cm^{-1} for HClO₄ to 895, 943, and 1131 cm^{-1} for HClO₄-H₂O, HClO₄–(H₂O)₂, and HClO₄–NH₃, respectively. All of these suggest the presence of strong hydrogen bonding. Both of the bending and torsional motions for the H atom of HClO₄ in the clusters become hindered as a result of hydrogen bonding, thereby increasing the bending and torsional force constants.

The harmonic frequencies of intramolecular modes for the clusters $HClO_4-(H_2O)_3$ and $HClO_4-NH_3-H_2O$ are found difficult to match to the frequencies of the monomers $HClO_4$, H_2O , and NH_3 . The most noticeable change is the disappearance of the OH stretching mode and the related bending of the torsional modes. While the intramolecular harmonic frequencies cannot be fully correlated with the isolated monomer modes for $HClO_4$, H_2O , and NH_3 , they can be more easily correlated with those of the ions ClO_4^- , NH_4^+ , and H_3O^+ , as shown in Table 4. This is consistent with the fact that the ionic dissociation of $HClO_4$ has occurred in the clusters $HClO_4-(H_2O)_3$ and $HClO_4-NH_3-H_2O$.

IV. Comparison to Sulfuric Acid

It is interesting to compare the clusters of perchloric acid with the corresponding clusters of sulfuric acid. The hydrated clusters of H₂SO₄ with up to five water molecules were studied by Re et al.³ using the B3LYP/D95++** method and by Larson et al.⁴ using the B3LYP and MP2 methods with the 6-311++G-(d,p) basis set. The clusters of H₂SO₄–NH₃ with up to two water molecules were studied by Larson and Tao⁸ using the B3LYP and MP2 methods with the 6-311++G(d,p) basis set. Our comparisons of the clusters between HClO₄ and H₂SO₄ focus primarily on the geometrical parameters and vibrational frequencies involving the acidic proton that donates a hydrogen bond to water or ammonia in the clusters. It may help us better understand the relative acidity between the two strong acids in aqueous conditions. Table 5 gives a summary of the comparisons between the two series of clusters for HClO₄ and H₂SO₄.

The two acids have very comparable OH bond distances in the monomers from B3LYP and MP2 calculations. Upon hydrogen bonding to water, the OH bond distances are both increased by a small, but nearly the same, magnitude. The increases in the OH bond distances are larger upon hydrogen bonding to ammonia than to water, but are nearly the same in magnitude between the two acids. Therefore, the changes in the OH bond lengths upon hydrogen bonding do not yield clear evidence to show the difference in acidity between the two acids. The same conclusion can be drawn from the comparison of the hydrogen bond distances r(H1O5) for the case of bonding to water and r(H1N) for the case of bonding to ammonia. The hydrogen bond distances are shorter in the ammonia systems than in the water systems, but virtually the same between the two acids, with either water or ammonia.

The two acids have nearly the same harmonic frequencies for the OH stretching mode in the monomers from B3LYP calculations. Large red shifts in the frequencies result from hydrogen bonding with water or ammonia, along with large enhancement in IR intensities. However, the HClO₄ acid gives a larger red shift than H₂SO₄, and the difference is more pronounced in the hydrogen-bonded systems with ammonia. This indicates that the weakening of the OH bond of HClO₄ is more severe than that of H₂SO₄ as the acid interacts with the proton acceptor (water or ammonia). In other words, HClO₄ is more acidic than H₂SO₄.

Proton transfer takes place in both HClO₄-NH₃-H₂O and $H_2SO_4-NH_3-H_2O_2$, producing the distinct cation NH_4^+ and the corresponding anions ClO₄⁻ and HSO₄⁻, respectively. This is demonstrated by the bond distances r(O1H1) and r(H1N). However, there are considerable differences in the bond distances between the two systems. r(O1H1) = 1.629 Å for $HClO_4-NH_3-H_2O$ is about 0.2 Å larger than that for $H_2SO_4-NH_3-H_2O$. On the other hand, r(H1N) = 1.061 Å for HClO₄–NH₃–H₂O is about 0.05 Å smaller than that for $H_2SO_4-NH_3-H_2O$. In each of the systems, the NH_4^+ cation becomes a Lewis acid and the anion (ClO₄⁻ or HSO₄⁻) becomes a Lewis base. The larger r(O1H1) distance for HClO₄-NH₃-H₂O than for $H_2SO_4-NH_3-H_2O$ indicates that ClO_4^- is a weaker base than HSO_4^- . The same conclusion can be drawn from the difference in r(H1N) between the two systems. That ClO_4^- is a weaker base than HSO₄⁻ corresponds to HClO₄ being a stronger conjugated acid than H₂SO₄. It is thus clear that the structures of HClO₄₋NH₃₋H₂O and H₂SO₄₋NH₃₋H₂O provide further strong evidence that HClO₄ is a stronger acid than H_2SO_4 .

The binding energies for the clusters involving HClO₄ are consistently larger than those for the corresponding clusters involving H₂SO₄. In general, the strength of a hydrogen bond formed between an acid and a base molecule, measured by the binding energy D_e of the resulting hydrogen-bonded clusters, increases with the acidity of the acid, or the hydrogen bond donor. Consequently, the larger values of D_e for the clusters involving HClO₄ than the corresponding values for H₂SO₄ further show that HClO₄ is the stronger acid.

In summary, the comparisons consistently show that $HClO_4$ is a stronger acid than H_2SO_4 , despite the insignificant differences in the structures of the monomers and clusters between the two acids. It should be pointed out that gas-phase deprotonization energies²⁰ calculated at the B3LYP/6-311++G(d,p) level also reflect the subtle difference in acidic strength between $HClO_4$ (300 kcal/mol) and H_2SO_4 (308 kcal/mol).

V. Conclusions

The equilibrium structures and other molecular properties are calculated for the clusters $HClO_4-(H_2O)_n$ (n = 1-3) and $HClO_4-NH_3-(H_2O)_n$ (n = 0, 1) using the B3LYP density functional method and MP2 ab initio method with extended basis sets. The clusters of $HClO_4$ with less than three water molecules are all strongly hydrogen-bonded. The $HClO_4$ molecule dissociates in the cluster with three water molecules and produces the H_3O^+ and ClO_4^- ion pair. The $HClO_4-NH_3$ system is also hydrogen-bonded while $HClO_4-NH_3-H_2O$ contains the NH_4^+ and ClO_4^- ion pair. The binding energies, dipole moments, and

harmonic vibrational frequencies of the clusters provide further support for the equilibrium structures.

Perchloric acid is very similar in acidity to sulfuric acid. The two acid molecules have very comparable OH bond distances and associated vibrational frequencies. They also result in nearly the same hydrogen bond structure with water and ammonia. However, the vibrational frequencies involving the acidic H atom in the hydrogen-bonded clusters and the ion pair structures in larger clusters, along with the binding energies of the various clusters, consistently show that $HClO_4$ is a stronger acid than H_2SO_4 .

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